SF2723 Topics in Mathematics III

Spring 2019

Introduction to Riemann Surfaces

Course Information

Course responsible: Jonatan Lenells, jlenells@kth.se

Course homepage: Available in Canvas, kth.instructure.com/courses/8099

Literature: S. Donaldson, Riemann Surfaces, Oxford University Press, 2011.

Course description: The course will cover Parts I-II, as well as selected parts of Parts III-IV, of Donaldson's book *Riemann Surfaces*. The table of contents is as follows:

Part I Preliminaries

- 1 Holomorphic functions
- 2 Surface topology

Part II Basic theory

- **3** Basic definitions
- 4 Maps between Riemann surfaces
- 5 Calculus on surfaces
- 6 Elliptic functions and integrals
- 7 Applications of the Euler characteristic

Part III Deeper theory

- 8 Meromorphic functions and the Main Theorem for compact Riemann surfaces
- 9 Proof of the Main Theorem
- 10 The Uniformisation Theorem

Part IV Further developments

- 11 Contrasts in Riemann surface theory
- 12 Divisors, line bundles and Jacobians
- 13 Moduli and deformations
- 14 Mappings and moduli
- 15 Ordinary differential equations

Prerequisites: A basic understanding of real and complex analysis and topology is expected.

Requirements/Grading: There will be homework assignments and, for students seeking a higher grade, an individual project. The individual project will involve writing a short paper on a topic of choice and an oral presentation. Grades will be assigned according to the following table:

Homework	Without project	With approved project
85-100%	С	A
60-84%	D	В
30-59%	E	С
0-29%	F	Fx