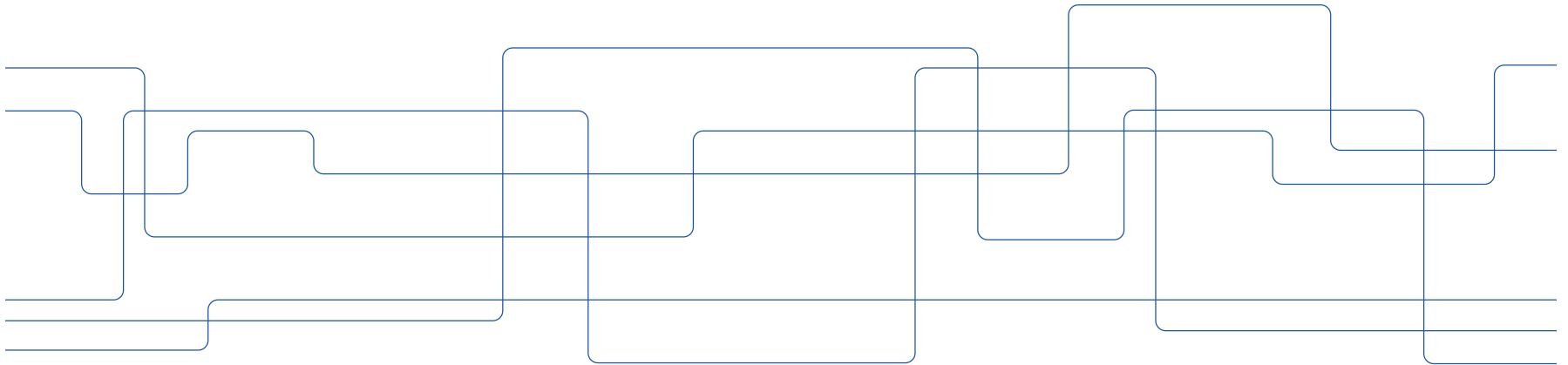


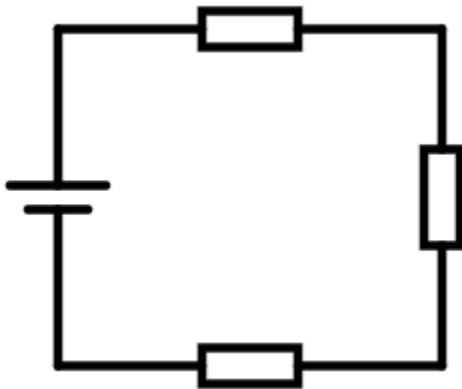


HE1027 Electrical Principals

Power in AC Current



Power in series and parallel



$$P_{\text{total}} = I_{\text{total}} * V_{\text{total}}$$

$$I_{\text{total}} = I_1 = I_2 = I_3$$

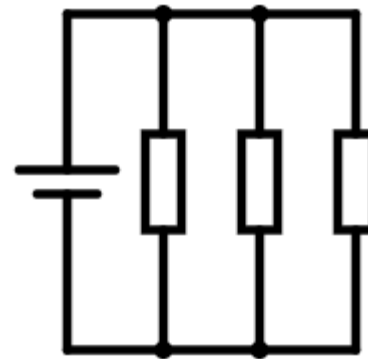
$$V_{\text{total}} = V_1 + V_2 + V_3$$

$$P_{\text{total}} = I_{\text{total}} * (V_1 + V_2 + V_3)$$

$$P_{\text{total}} = I_{\text{total}} * V_1 + I_{\text{total}} * V_2 + I_{\text{total}} * V_3$$

$$P_{\text{total}} = I_1 * V_1 + I_2 * V_2 + I_3 * V_3$$

$$P_{\text{total}} = P_1 + P_2 + P_3$$



$$P_{\text{total}} = I_{\text{total}} * V_{\text{total}}$$

$$V_{\text{total}} = V_1 = V_2 = V_3$$

$$I_{\text{total}} = I_1 + I_2 + I_3$$

$$P_{\text{total}} = (I_1 + I_2 + I_3) * V_{\text{total}}$$

$$P_{\text{total}} = V_{\text{total}} * I_1 + V_{\text{total}} * I_2 + V_{\text{total}} * I_3$$

$$P_{\text{total}} = V_1 * I_1 + V_2 * I_2 + V_3 * I_3$$

$$P_{\text{total}} = P_1 + P_2 + P_3$$



Real Power (aktiv effekt)

The actual amount of power being used, or dissipated, in a circuit is called real power

It is measured in watts (symbolized by the capital letter P, as always)

$$P = VI \cos \theta$$

$\theta=0^\circ$ for purely resistive

$\theta=90^\circ$ for purely inductive

$\theta=-90^\circ$ for purely capacitive





Reactive Power (reaktiv effekt)

- Inductors and capacitors do not decrease power
- They cause drops of voltage and draws of current that creates impression that they actually use power
- This “phantom power” is called reactive power
- It is measured in a unit called Volt-Amps-Reactive (VAR)
- The mathematical symbol for reactive power is the capital letter Q

$$Q=V I \sin \theta$$

$$Q=I^2 X$$

$$Q=V^2/X$$

Apparent Power (skenbar effekt)

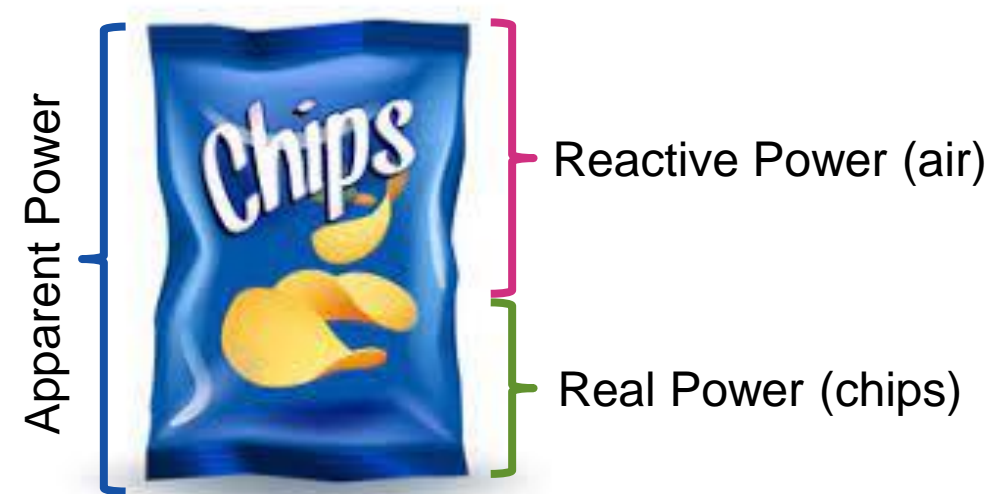
- The combination of real power and reactive power is called apparent power
- It is the product of a circuit's voltage and current, without reference to phase angle
- Apparent power is measured in the unit of Volt-Amps (VA) and is symbolized by the capital letter S

$$S=VI$$

$$S=P/\cos\theta$$

$$S=P+Qi \text{ for inductive load}$$
$$S=P-Qi \text{ for conductive load}$$

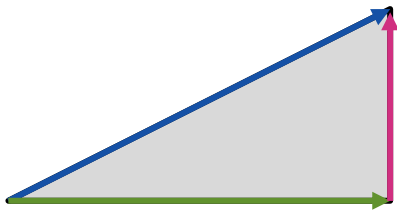
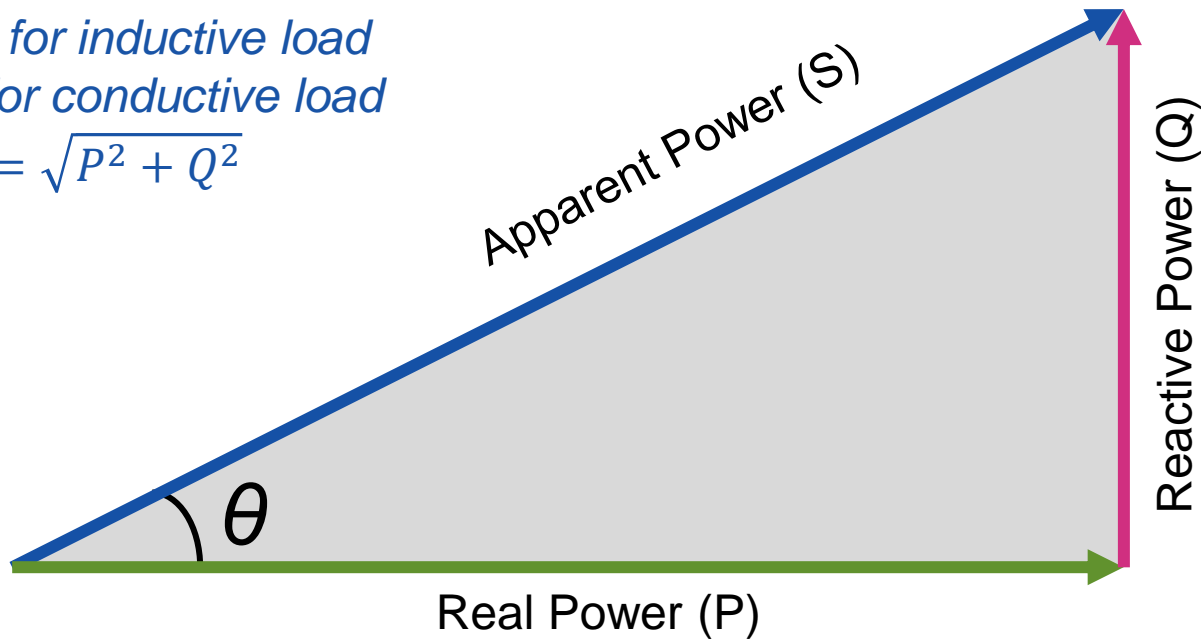
$$S = \sqrt{P^2 + Q^2}$$



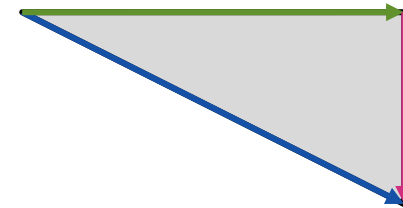
Power Diagram

From previous slide:

$$S = P + Qi \text{ for inductive load}$$
$$S = P - Qi \text{ for capacitive load}$$
$$S = \sqrt{P^2 + Q^2}$$



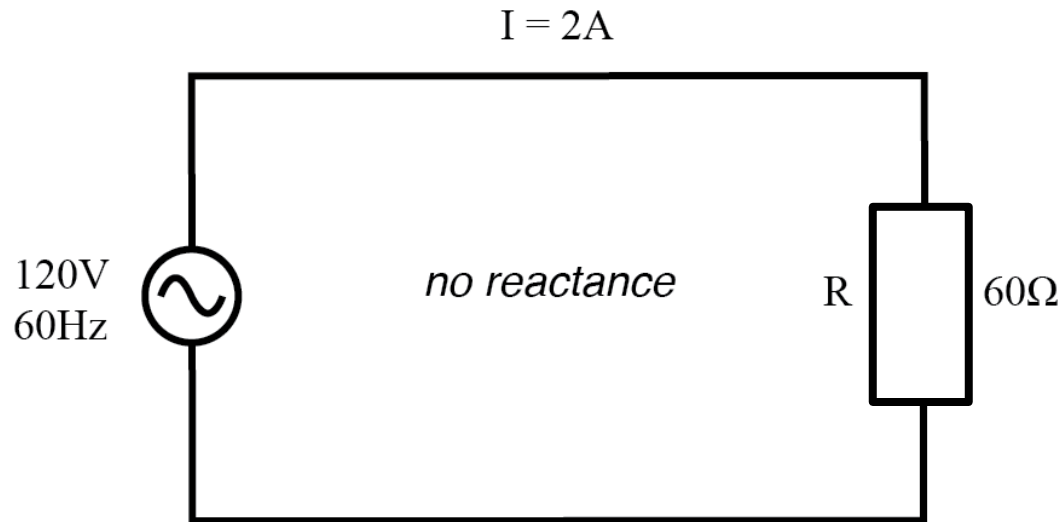
Power diagram for inductive load



Power diagram for capacitive load

Example

Find P , Q and S



$$\text{Real power } P = VI \cos \theta = 120 \cdot 2 \cdot 1 = 240 \text{ W}$$

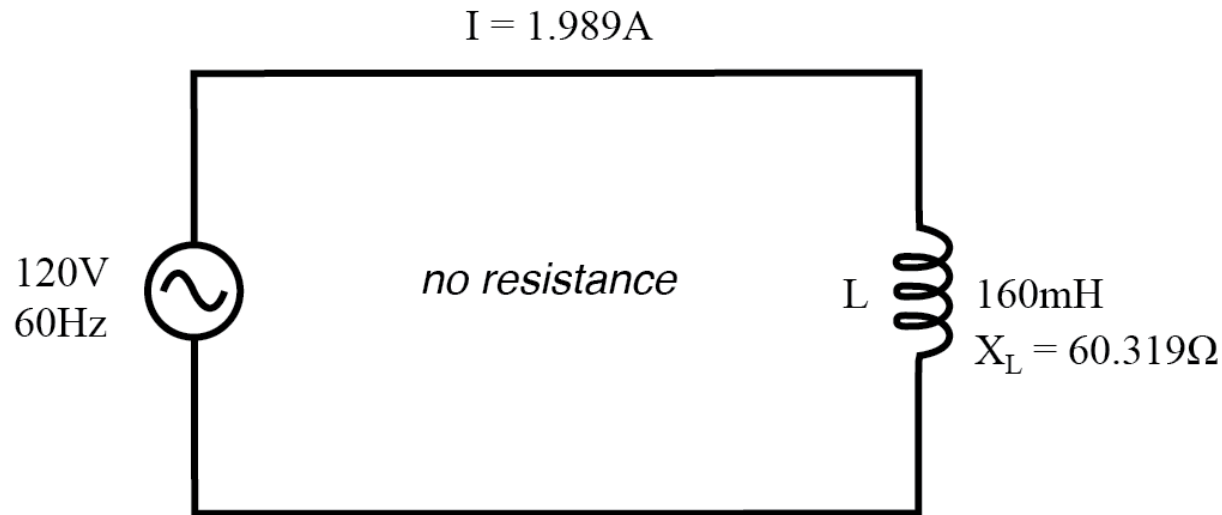
since it is a resistive network $\cos \theta = 1$ and $\sin \theta = 0$

$$\text{Reactive power } Q = VI \sin \theta = 120 \cdot 2 \cdot 0 = 0 \text{ VAR}$$

$$\text{Apparent power } S = 240 + 0i = 240 \text{ VA}$$

Example

Find P , Q and S



$$\text{Real power } P = VI \cos \theta = 120 \cdot 1.989 \cdot 0 = 0\text{W}$$

$$\text{Reactive power } Q = VI \sin \theta = 120 \cdot 1.989 \cdot 1 = 238.73\text{VAR}$$

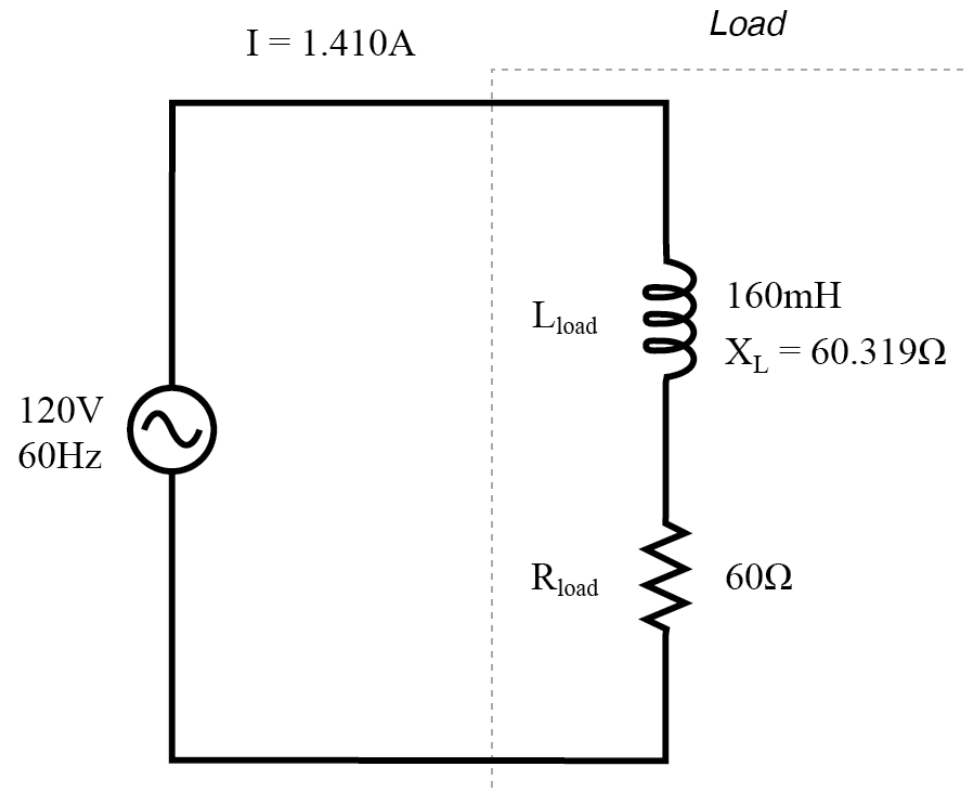
$$Q = I^2 X = 1.989^2 \cdot 60.319 = 238.6\text{VAR}$$

$$Q = V^2 / X = 120^2 / 60.319 = 238.73\text{VAR}$$

$$\text{Apparent power } S = VI = 120 \cdot 1.989 = 238.73\text{VA}$$

Example

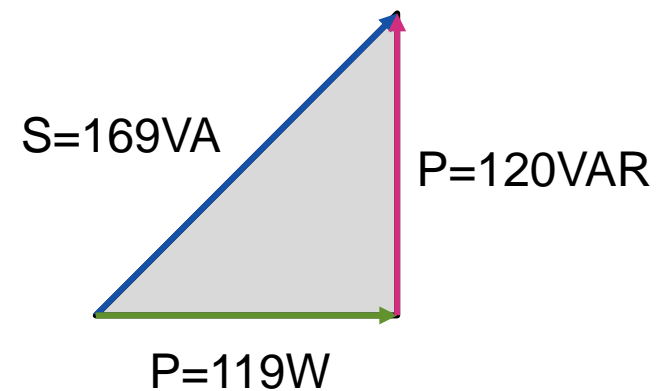
Find P , Q and S



Real power $P = I^2 R = 119.395\text{W}$

Reactive power $Q = I^2 X = 119.998\text{VAR}$

Apparent power $S = 119.395 + 119.998i$





Power Factor

Since $P=VI\cos\theta$ and $S=VI$, $P=S\cos\theta$

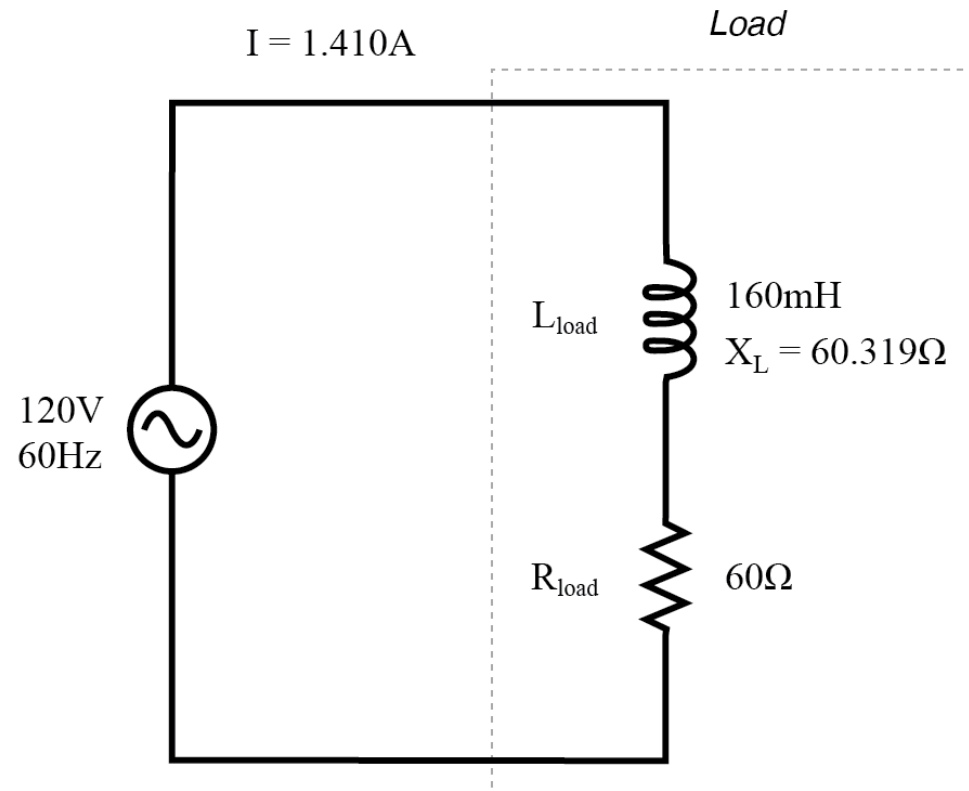
$$\cos \theta = \frac{P}{S}$$

A ratio of the real power to apparent power ($\cos\theta$)
is known as power factor



Example

Find power factor



Real power $P = I^2 R = 119.395\text{W}$

Reactive power $Q = I^2 X = 119.998\text{VAR}$

Apparent power $S = 119.395 - 119.998i \text{ VA}$

$$\cos \theta = \frac{P}{S} = \frac{119}{169} = 0.704 = 70.4\%$$



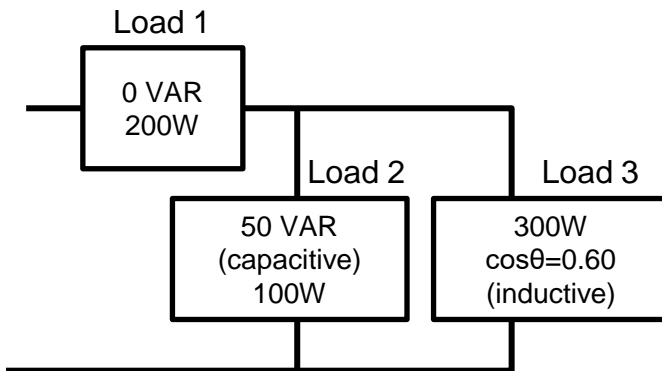
P_{Total} , Q_{Total} and S_{Total}

1. Find the real power and reactive power for each branch of the circuit.
 2. The total real power of the system P_{Total} is then a sum of average power delivered to each branch
 3. The total reactive power Q_{Total} is the difference between the reactive power of the inductive loads and that of the capacitive loads
 4. The total apparent power $S_T = \sqrt{P_{\text{Total}}^2 + Q_{\text{Total}}^2}$
 5. The total power factor is $\cos \theta = \frac{P_{\text{Total}}}{S_{\text{Total}}}$
-



Example

Find S_{Total} and power factor



1. Find P and Q for each element

$$P_1 = 200W \text{ and } Q_1 = 0VAR$$

$$P_2 = 100W \text{ and } Q_2 = -50VAR \text{ (cap)}$$

$$P_3 = 300W$$

$$\cos\theta = P/S \rightarrow S_3 = P_3 / \cos\theta_3 = 300 / 0.6 = 500VA$$

$$Q = VI\sin\theta = S\sin\theta$$

$$\theta_3 = \arccos(0.6) = 53.13^\circ$$

$$Q_3 = 500 * \sin(53.13^\circ) = 500 * 0.8 = +400VAR \text{ (induc)}$$

2. Find real power P_{Total}

$$P_{Total} = P_1 + P_2 + P_3 = 200 + 100 + 300 = 600W$$

3. Find reactive power Q_{Total}

$$Q_{Total} = Q_1 - Q_2 + Q_3 = 0 - 50 + 400 = 350VAR \text{ (induc)}$$

cap induc

4. Find apparent power S_{Total}

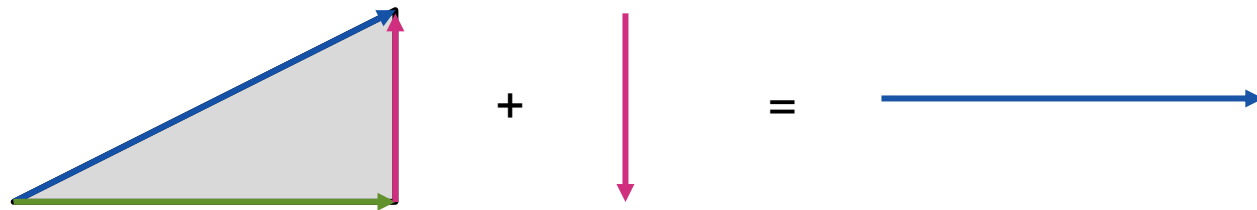
$$S_{Total} = \sqrt{600^2 + 350^2} = 695VA$$

5. Find power factor

$$\cos\theta = \frac{600}{695} = 0.86 \text{ (inductive)}$$

Power Factor Correction

- Reactive power leads to power losses
- To decrease the reactive power, we need to have power factor as close to 1 as possible
- The process of introducing reactive element to bring the power factor closer to 1 is called power factor correction



To correct inductive load we add a capacitor and to improve capacitive load we add inductor



Example

Find a value for an element to increase power factor to 1

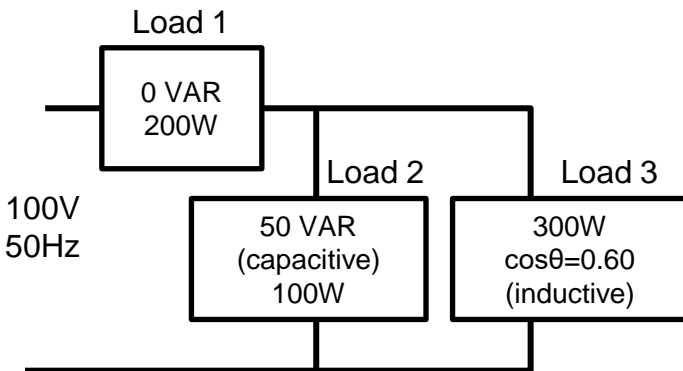
Since loads in total are inductive, we need to add a capacitor to remove all reactive power.

So we need to get away of $Q=350\text{VAR}$

We know that $Q=V^2/X$ or $X_C=V^2/Q$

$$X_C=100^2/350=28.57\Omega$$

$$C = \frac{1}{2\pi f X_C} = \frac{1}{2\pi \cdot 50\text{Hz} \cdot 28.57\Omega} = 1.11 \cdot 10^{-4}\text{F} = 111\mu\text{F}$$



$$P_{\text{Total}}=600\text{W}$$

$$Q_{\text{Total}}=350\text{VAR (inductive)}$$

$$S_{\text{Total}}=695\text{VA}$$

$$\cos\theta=0.86 \text{ (inductive)}$$



Example

Find a value for an element to increase power factor to 0.95

Since loads in total are inductive, we need to add a capacitor

$$\cos \theta' = 0.95 = \frac{P}{S}$$

P stays the same, so new $S' = \frac{P}{0.95} = \frac{600}{0.95} = 631,58\text{VA}$

$$\theta' = \cos^{-1}(0.95) = 18,19^\circ$$

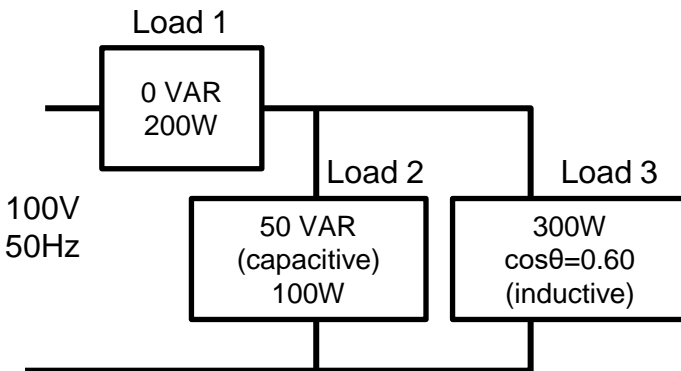
$$\text{New } Q' = S' \sin(\theta') = 631,58 \cdot \sin(18,19^\circ) = 631,58 \cdot 0.312 = -197.21\text{VAR}$$

So we need to get away of $\Delta Q = 350 - 197.21 = 152.79\text{VAR}$

We know that $Q = V^2/X$ or $X_C = V^2/Q$

$$X_C = 100^2 / 152.79 = 65.45\Omega$$

$$C = \frac{1}{2\pi f X_C} = \frac{1}{2\pi \cdot 50\text{Hz} \cdot 65.45\Omega} = 4.86 \cdot 10^{-5}\text{F} = 49\mu\text{F}$$

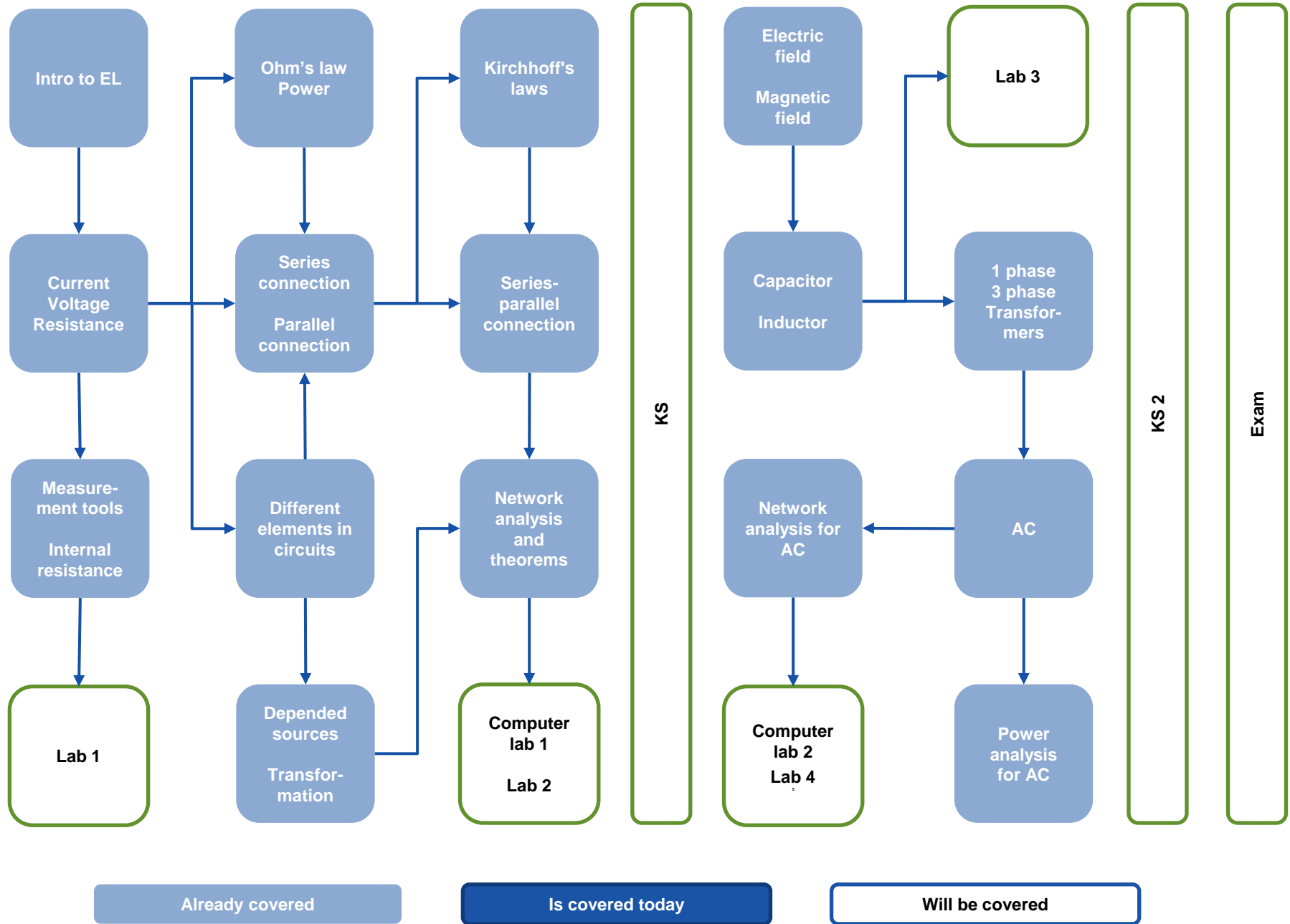


$$P_{\text{Total}} = 600\text{W}$$

$$Q_{\text{Total}} = 350\text{VAR (inductive)}$$

$$S_{\text{Total}} = 695\text{VA}$$

$$\cos\theta = 0.86 \text{ (inductive)}$$





Suggested reading

Introductory Circuit Analysis

– Kap 20: **20.1 - 20.9**



Suggested exercises

- Kap 20: 11, 14, 15, 17, 18, 19