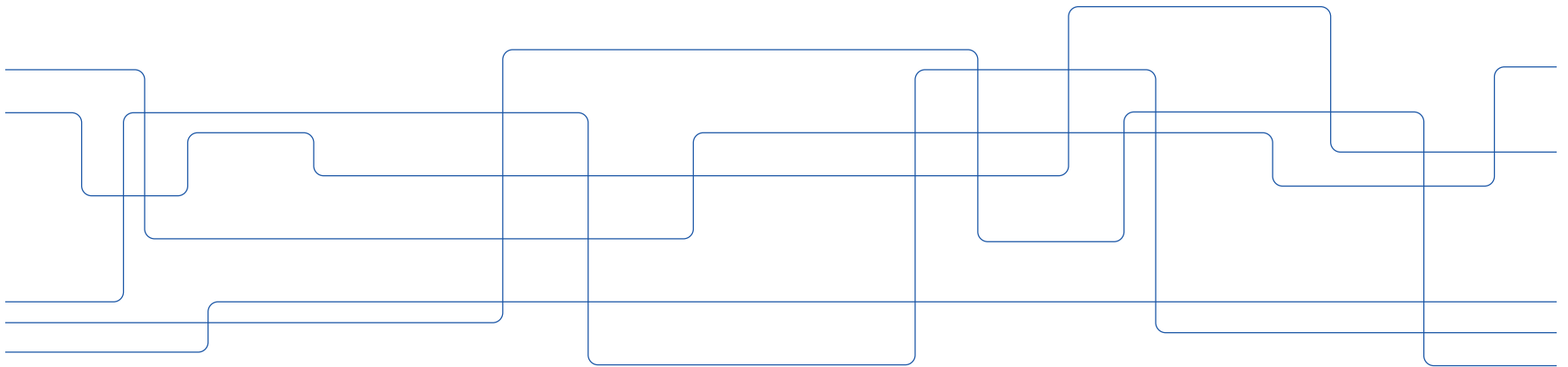
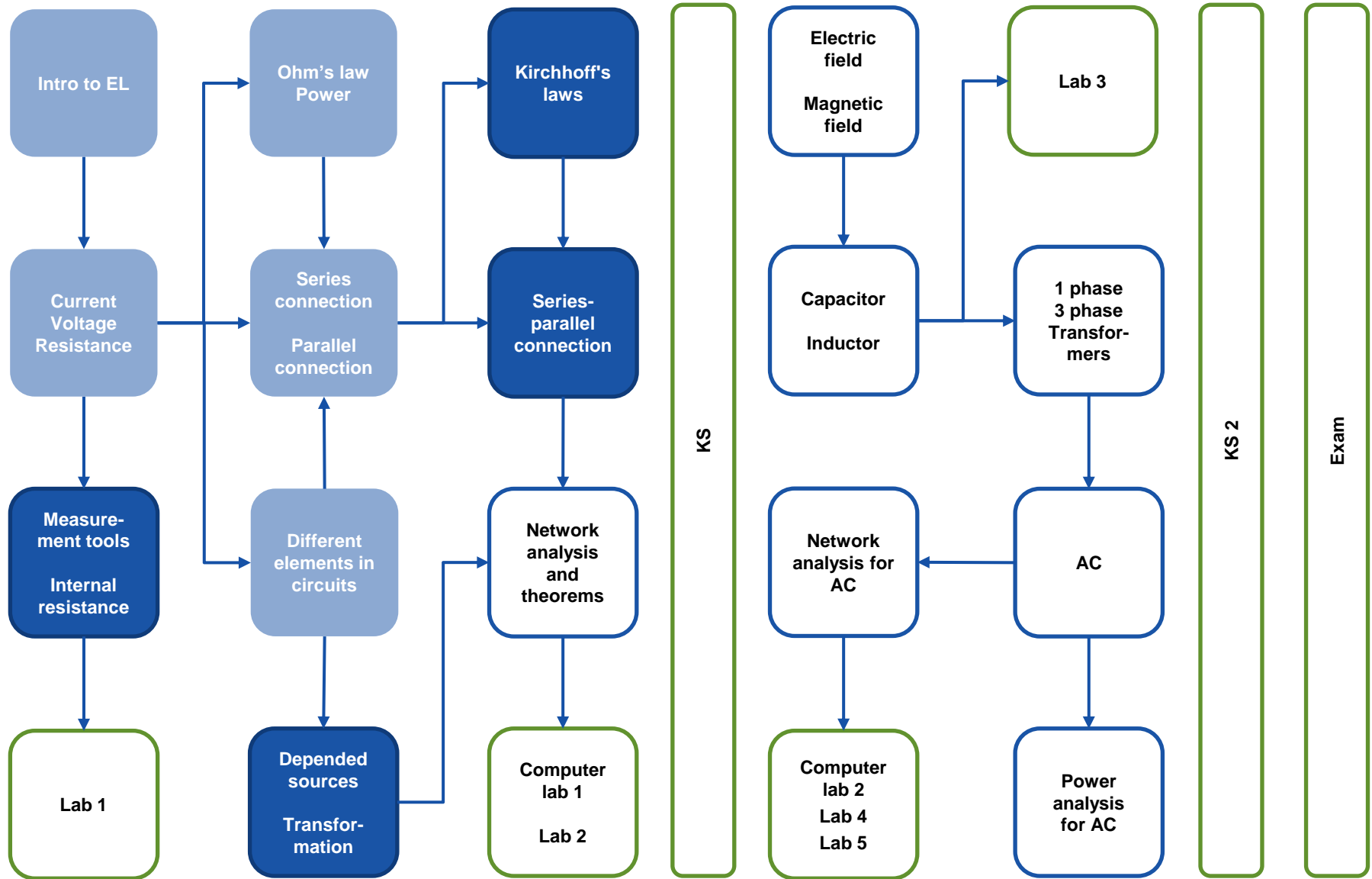




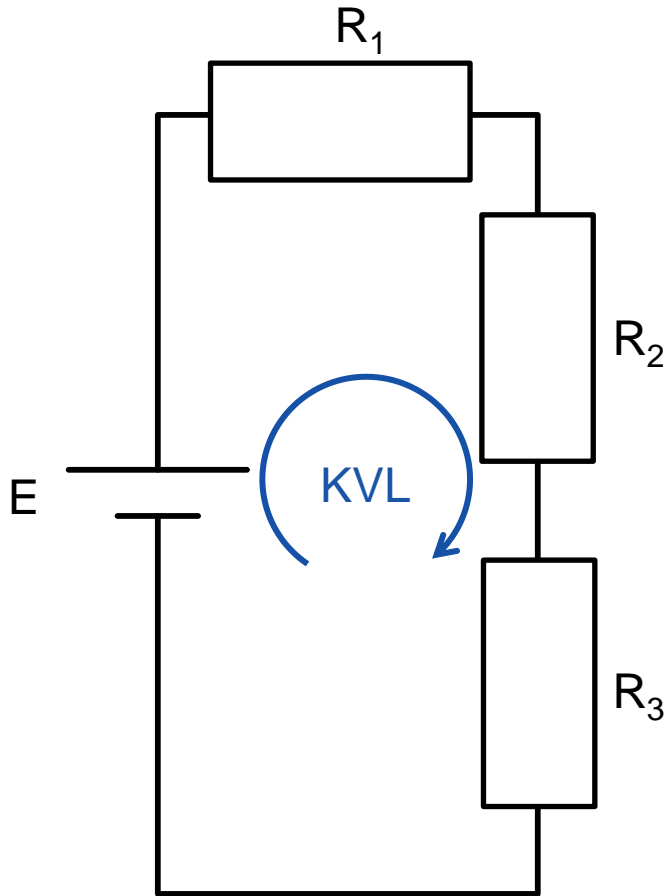
# HE1027 Electrical Principals

## Lecture 2: Series-Parallel Circuits Exercises





## Series Circuits – Kirchhoff's Voltage Law



- The sum of all potential rises (sources) and drops (consumptions) around a closed path is zero

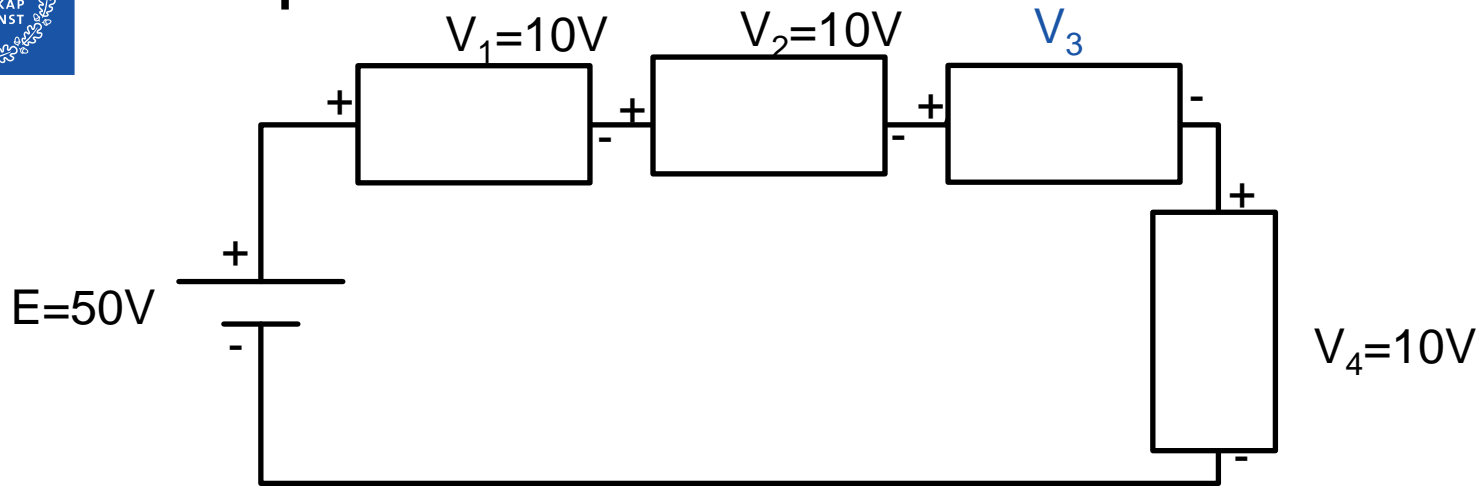
$$E + V_1 + V_2 + V_3 = 0 \quad (V_1 \ V_2 \ V_3 \text{ has negative values})$$

$$E = V_1 + V_2 + V_3 \quad (V_1 \ V_2 \ V_3 \text{ has positive values})$$

$$\sum E = \sum V$$

---

## Example



*What is  $V_3$  voltage?*

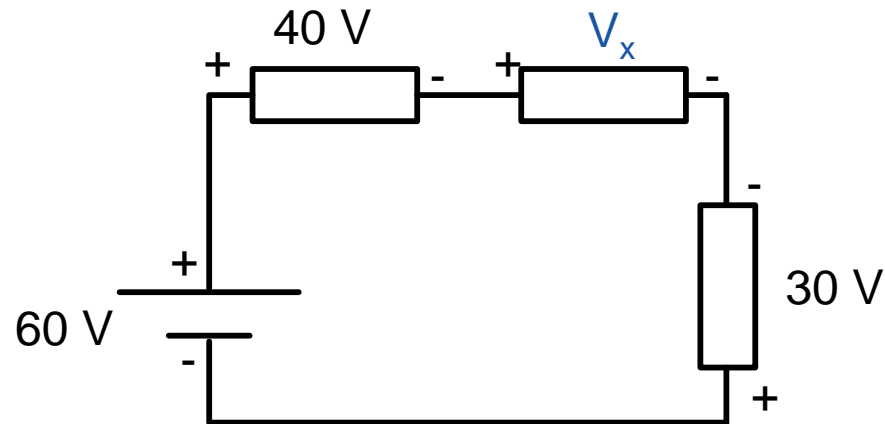
$$E = V_1 + V_2 + V_3 + V_4 \quad \text{or} \quad E - V_1 - V_2 - V_3 - V_4 = 0$$
$$50 = 10 + 10 + V_3 + 10$$

$$V_3 = 50 - 10 - 10 - 10 = 20V$$

*Determine a current if  $R_3$  is  $40\Omega$ ?*

$$I = \frac{V_3}{R_3} = \frac{20}{40} = 0,5A$$

## Example



*Blocks represent mixtures of components. Determine the unknown voltage*

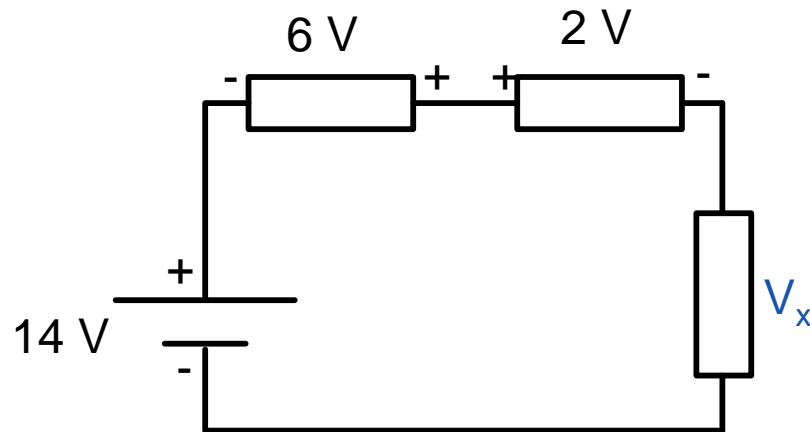
$$60 - 40 - V_x + 30 = 0$$

$$-V_x = -60 + 40 - 30 = -50$$

$$V_x = 50 \text{ V}$$

---

## Example



*Determine the unknown voltage and polarity*



*(randomly selected)*

$$14 + 6 - 2 - V_x = 0$$

$$V_x = 18V$$

Polarity was selected correct



*(randomly selected)*

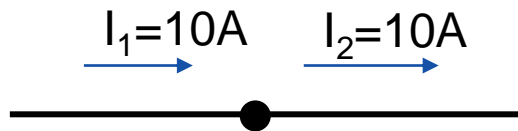
$$14 + 6 - 2 + V_x = 0$$

$$V_x = -18V$$

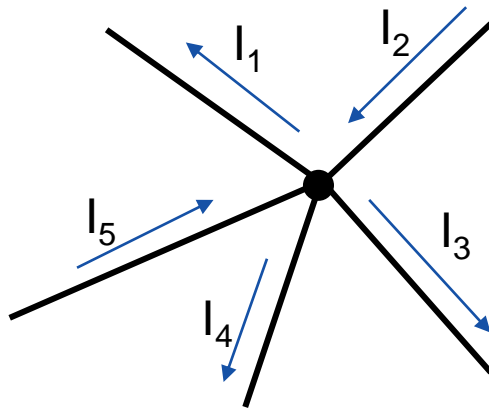
Polarity was selected incorrect and should be reversed

# Kirchhoff's Current Law

- The sum of currents entering and leaving a junction or region of network is zero

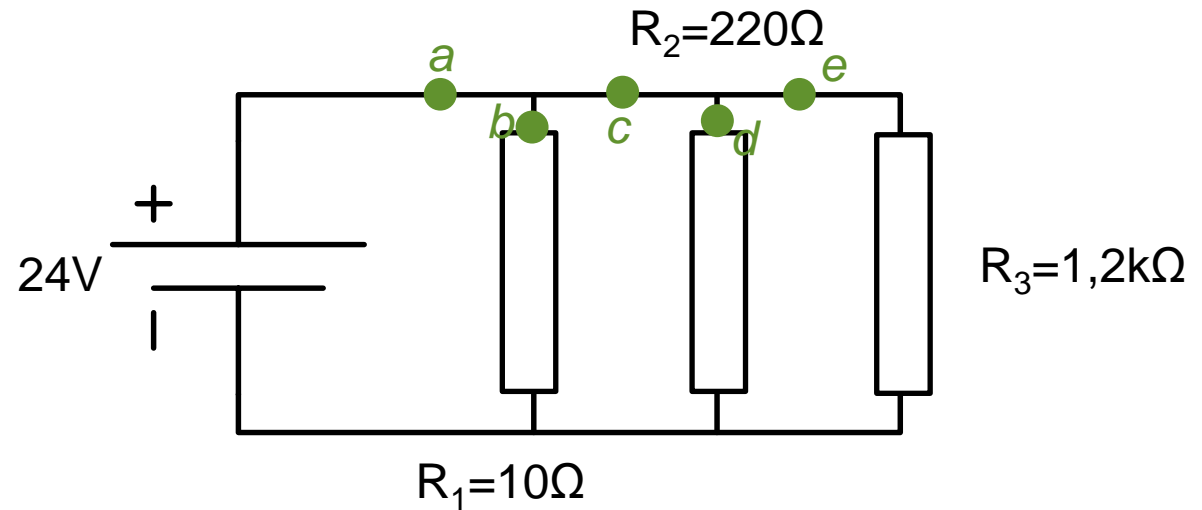


$$I_1 + I_2 = 0 \quad (\text{if } I_2 \text{ is negative})$$
$$I_1 - I_2 = 0 \quad (\text{if } I_2 \text{ is positive})$$



$$-I_1 + I_2 - I_3 - I_4 + I_5 = 0$$

## Example



*Determine the current in points a, b, c, d and e*

Prom previous lecture we know that

$$I_a = 2,53 \text{ A}$$

$$I_b = 2,4 \text{ A}$$

$$I_c = 0,11 \text{ A}$$

$$I_d = 0,02 \text{ A}$$

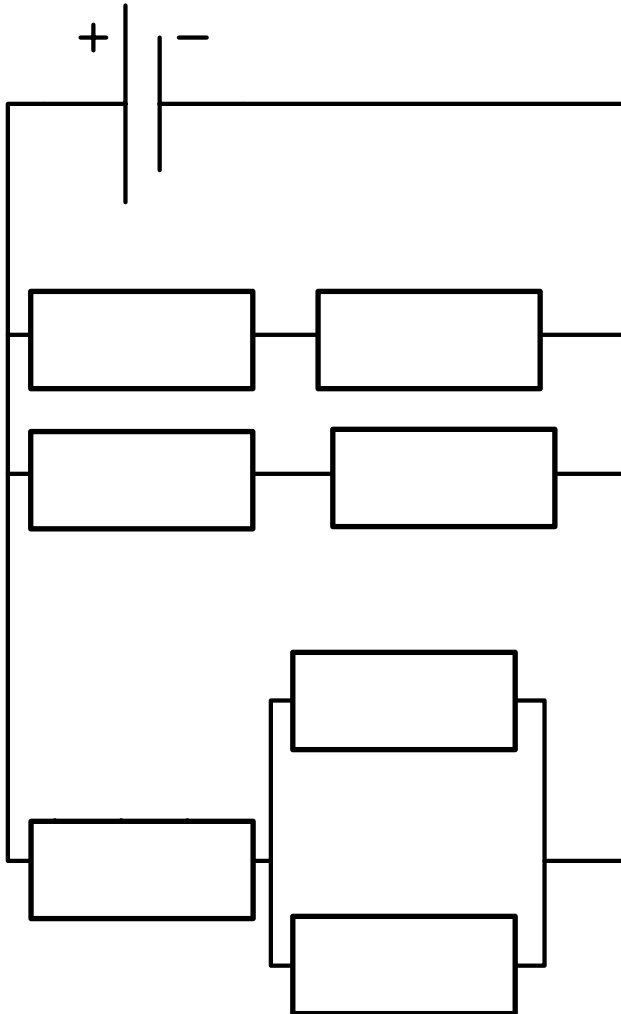
$$I_c = I_a - I_b = 0,13 \text{ A}$$

or

$$I_c = I_d + I_e = 0,13 \text{ A}$$



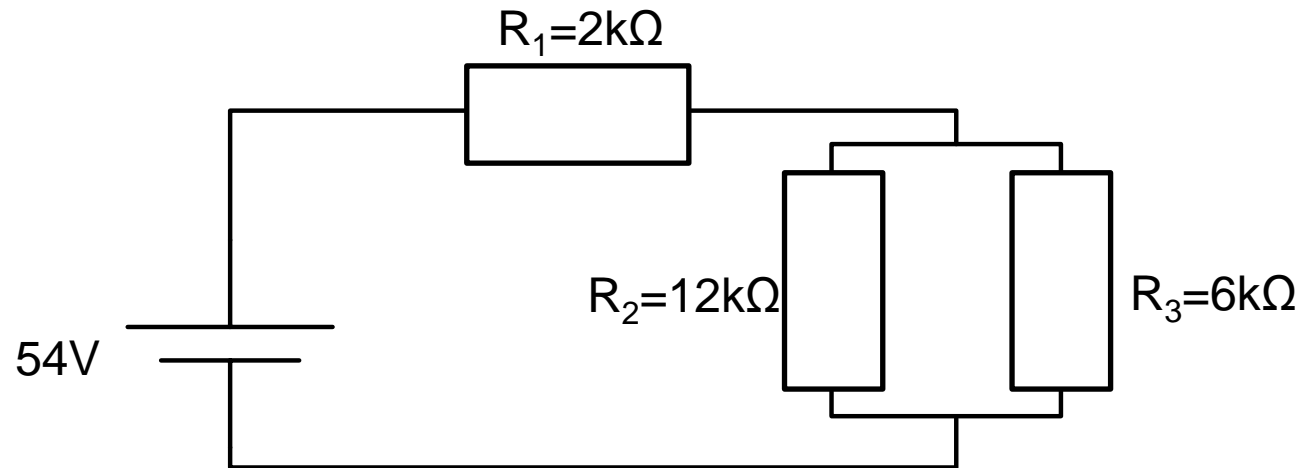
## Series-Parallel Circuits



- Most of circuits are combination of series connections and parallel connections
- To solve it we can use reduce and return approach:
  - find and solve elements that are just series or just parallel
  - (mentally) redraw these elements as one
  - repeat until all is reduced to one element
  - now redraw circuit back to original based on found values

## Example 1

$$R_{Total \text{ for parallel resistors}} = \frac{R_x \cdot R_y}{R_x + R_y}$$



Find current  $I_3$

$$R_T = R_1 + \frac{R_2 \cdot R_3}{R_2 + R_3} = 2 + \frac{12 \cdot 6}{12 + 6} = 2 + 4 = 6k\Omega$$

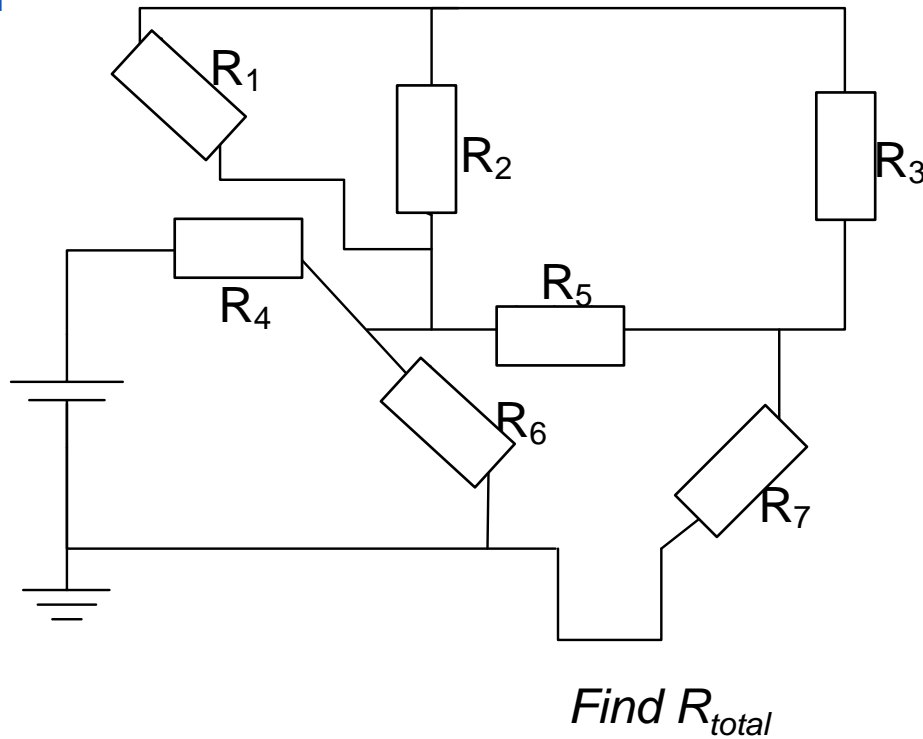
$$I_T = \frac{54}{6000} = 9mA$$

$$V_1 = I_T \cdot R_1 = 9mA \cdot 2k\Omega = 18V$$

$$V_3 = V_2 = E - V_1 = 54 - 18 = 36V$$

$$I_3 = \frac{V_3}{R_3} = 6mA$$

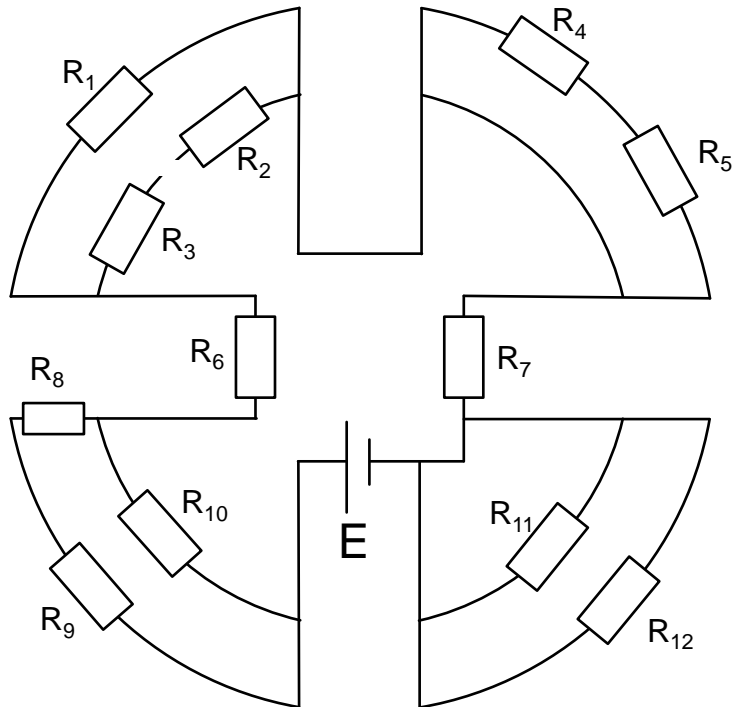
## Example 2



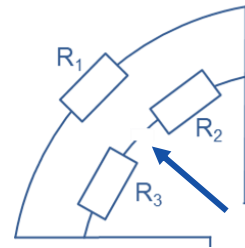
Parallel  $R_a // R_b$   
Serial  $R_a + R_b$

$$R_T = (((R_1 // R_2) + R_3) // R_5 + R_7) // R_6 + R_4$$

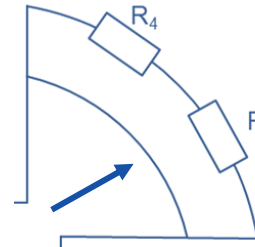
## Example 3



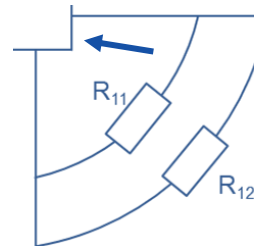
Find  $R_{total}$



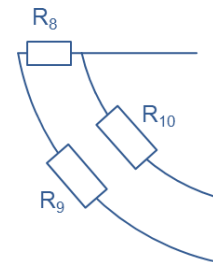
$R_T = R_1$   
 $R_2$  and  $R_3$  are open circuit



$R_T = 0$   
 $R_4$  and  $R_5$  are closed circuit



$R_T = 0$   
 $R_{11}$  and  $R_{12}$  are closed circuit



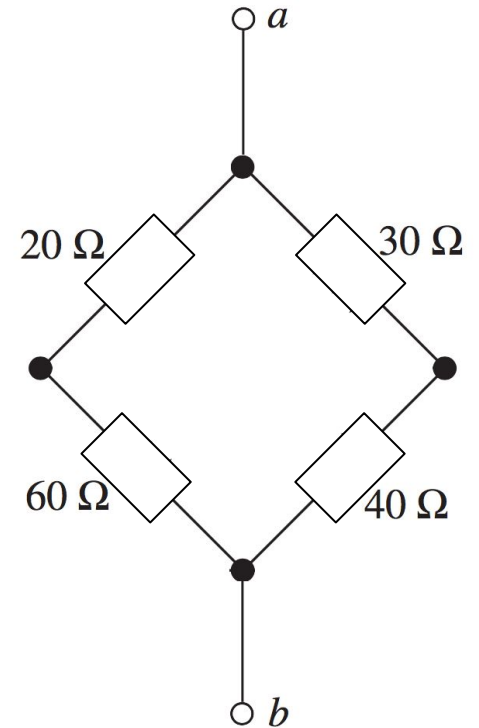
$R_T = (R_8 + R_9) // R_{10}$

$$R_T = R_1 + R_7 + (R_8 + R_9) // R_{10} + R_6$$

## Example 4

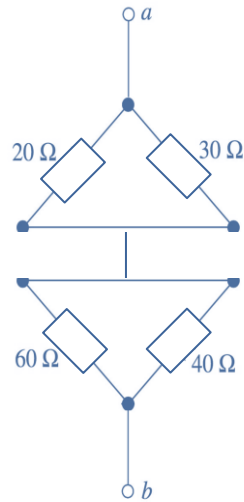
Find resistance between  $a$  and  $b$

$$R_T = (20 + 60) // (30 + 40)$$

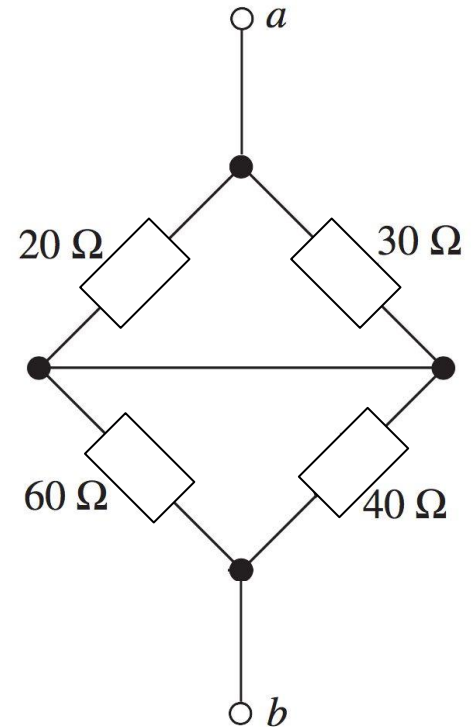


## Example 5

Find resistance between  $a$  and  $b$

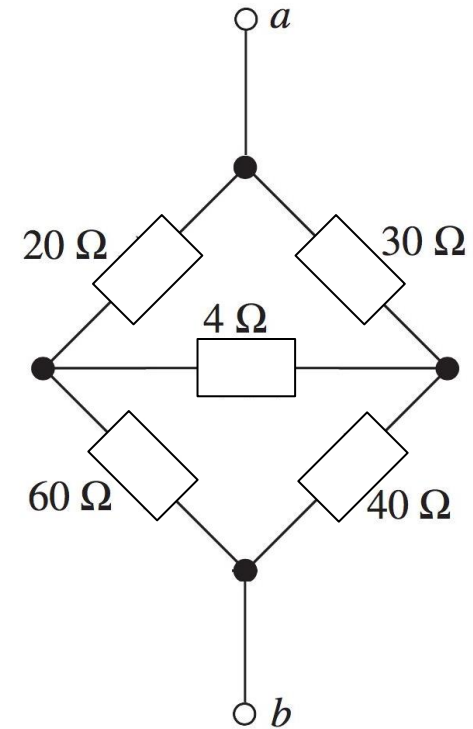


$$R_T = 20 // 30 + 60 // 40$$



## Example 6

Find resistance between  $a$  and  $b$



?

# Delta-Wye transformation

$$Z_1 = \frac{Z_{12} \cdot Z_{13}}{Z_{12} + Z_{13} + Z_{23}}$$

$$Z_2 = \frac{Z_{12} \cdot Z_{23}}{Z_{12} + Z_{13} + Z_{23}}$$

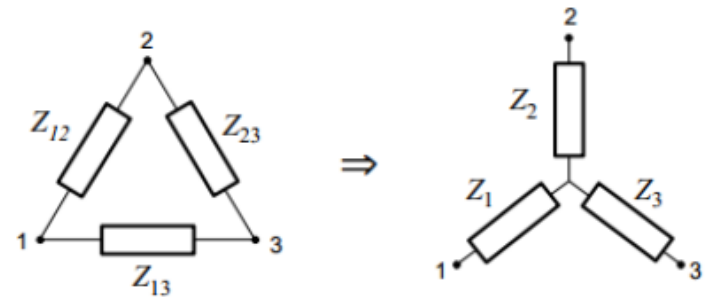
$$Z_3 = \frac{Z_{13} \cdot Z_{23}}{Z_{12} + Z_{13} + Z_{23}}$$

$$Z_{12} = Z_1 \cdot Z_2 \sum_{i=1}^3 \frac{1}{Z_i}$$

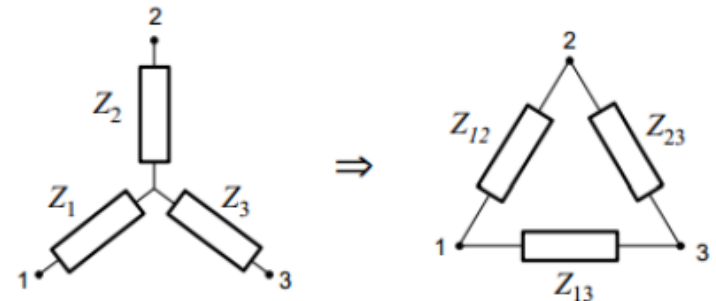
$$Z_{13} = Z_1 \cdot Z_3 \sum_{i=1}^3 \frac{1}{Z_i}$$

$$Z_{23} = Z_2 \cdot Z_3 \sum_{i=1}^3 \frac{1}{Z_i}$$

Triangel – Stjärntransformation/ D - Y



Stjärn – Triangeltransformation/ Y - D

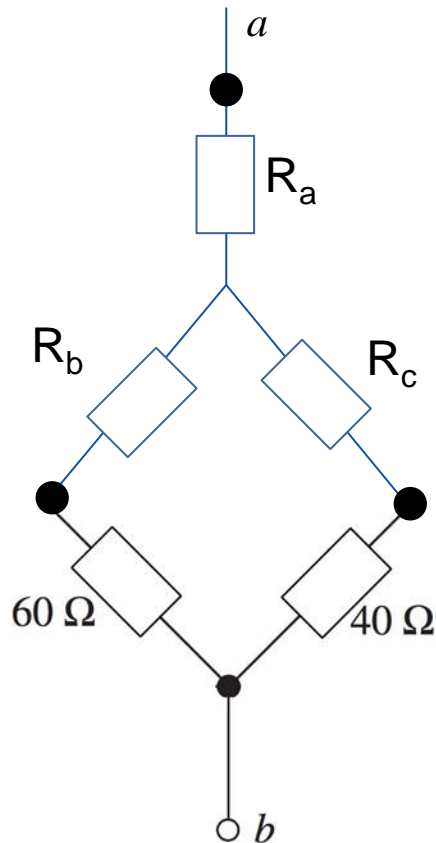




## Example 6

Find resistance between  $a$  and  $b$

Transforming top triangle into star:  $R_1 = \frac{R_{12} \cdot R_{13}}{R_{12} + R_{13} + R_{23}}$

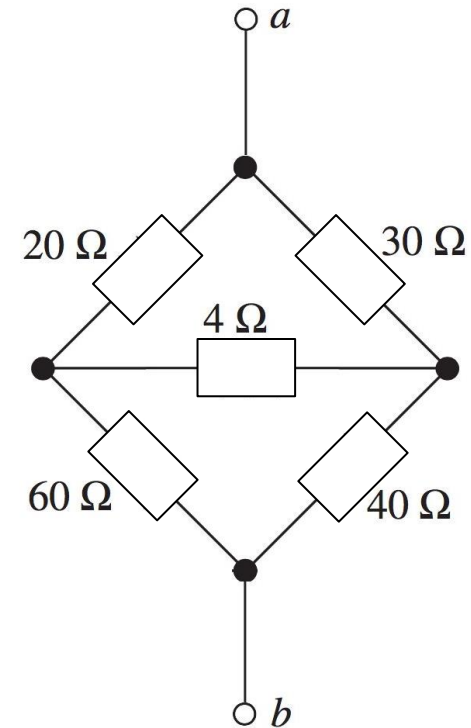


$$R_a = \frac{20 \cdot 30}{20 + 30 + 4} = 11\Omega$$

$$R_b = \frac{20 \cdot 4}{20 + 30 + 4} = 1,482\Omega$$

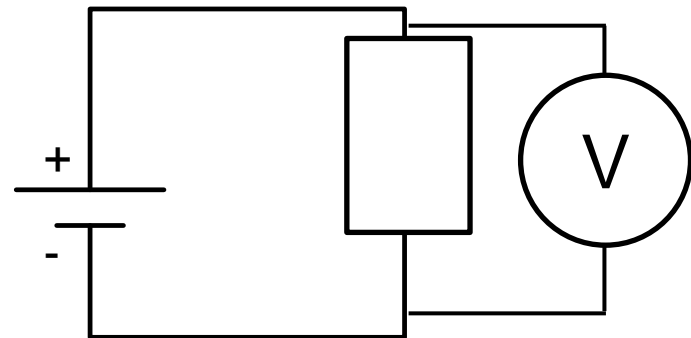
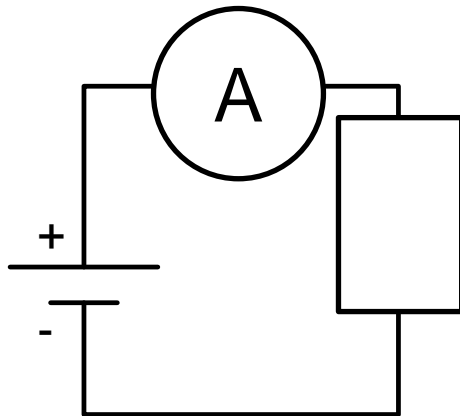
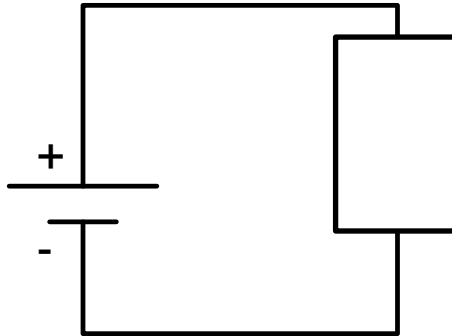
$$R_c = \frac{30 \cdot 4}{20 + 30 + 4} = 2,222\Omega$$

$$R_T = 11 + (1,482 + 60) // (2,222 + 40)$$



# Measuring tools

- Based on series or parallel – how should measuring tools be connected?





# Internal resistance

- A voltmeter needs some current to flow to measure
  - It should not change the amount of current going through the element between those two points
  - The less current is better to avoid affecting the circuit
  - Digital voltmeters today have an input resistance of 10 Megohms or more
  - Wrong readings in circuits with high resistance
- 
- Ammeters tend to influence the amount of current in the circuits they're connected to
  - The ideal ammeter has zero internal resistance, so as to drop as little voltage as possible
  - Wrong readings in circuits with low resistance
-

# Electricity Sources in Circuits

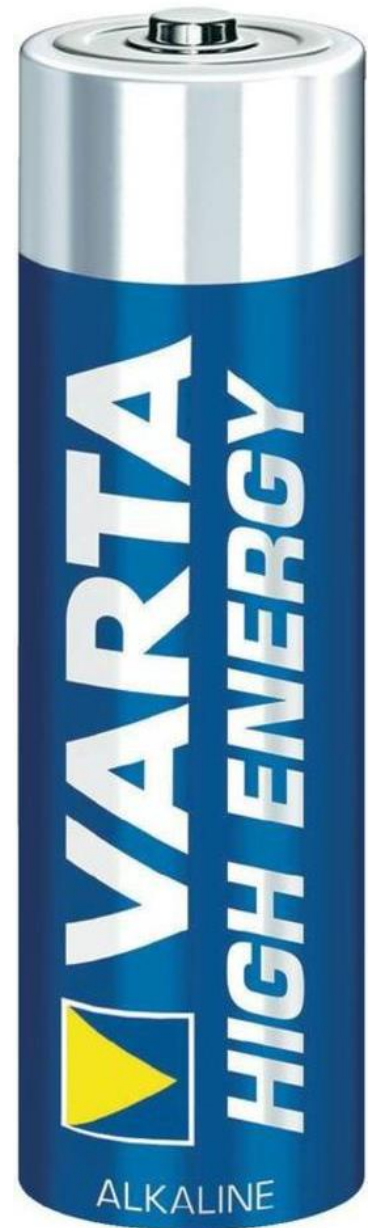
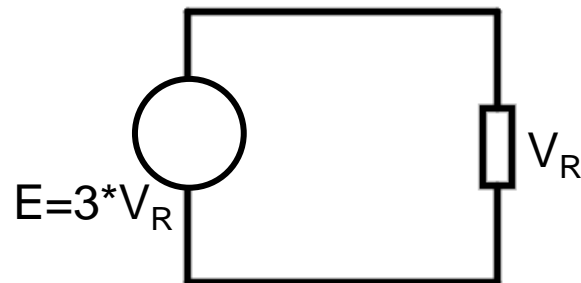
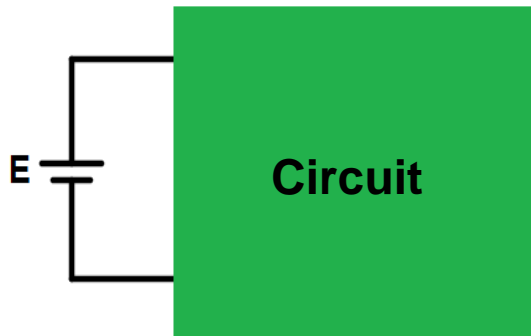
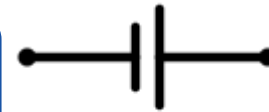
**Sources**

Voltage sources

Current sources

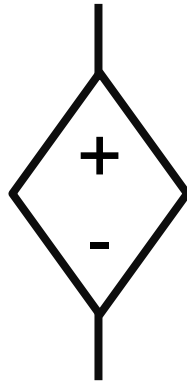
Independent  
source

Dependent  
source



## Dependent Source

The source output value depends upon the voltage or current at some other part of the circuit



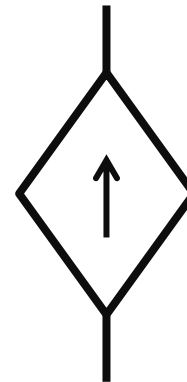
Dependent voltage source

Voltage Controlled  
Voltage Source

$$V = a * V_b$$

Current Controlled  
Voltage Source

$$V = a * I_b$$



Dependent current source

Current Controlled  
Current Source

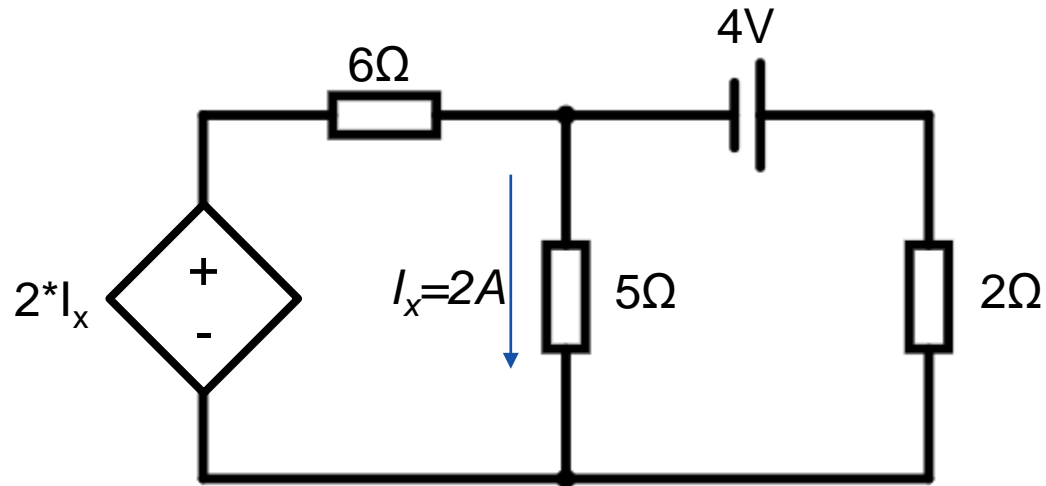
$$I = a * I_b$$

Voltage Controlled  
Current Source

$$I = a * V_b$$

## Example

*Determine type and voltage of the dependent source*

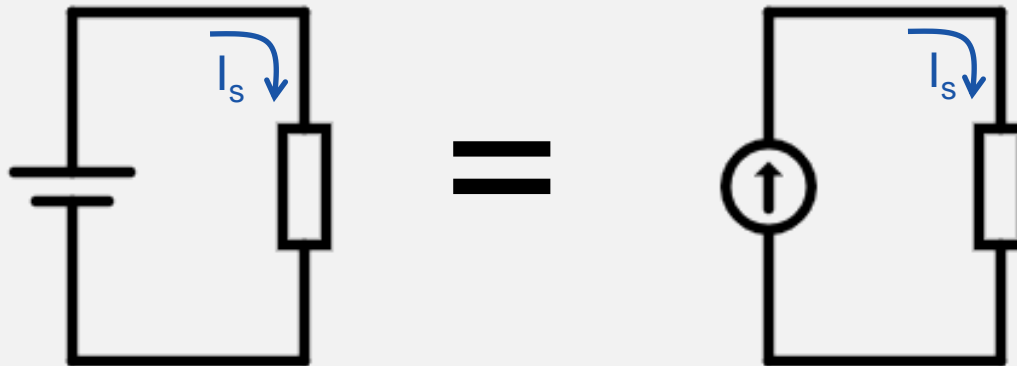


Current Controlled Voltage Source (CCVS)

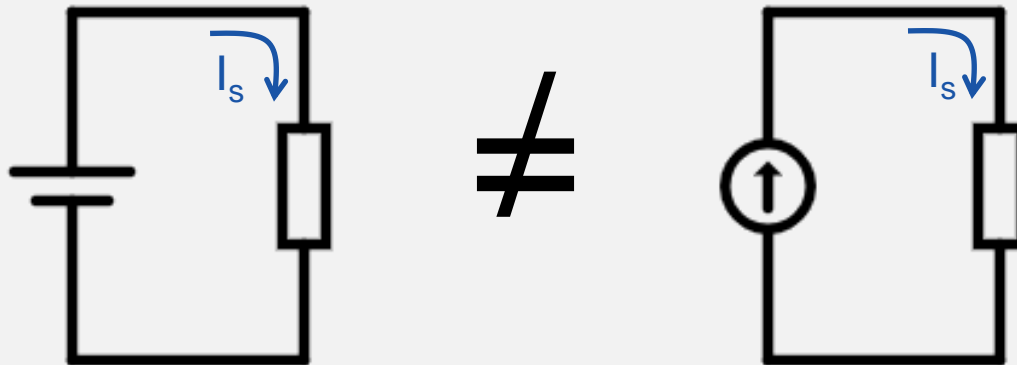
$$E = 2 \cdot 2 = 4V$$

---

## Source Conversion

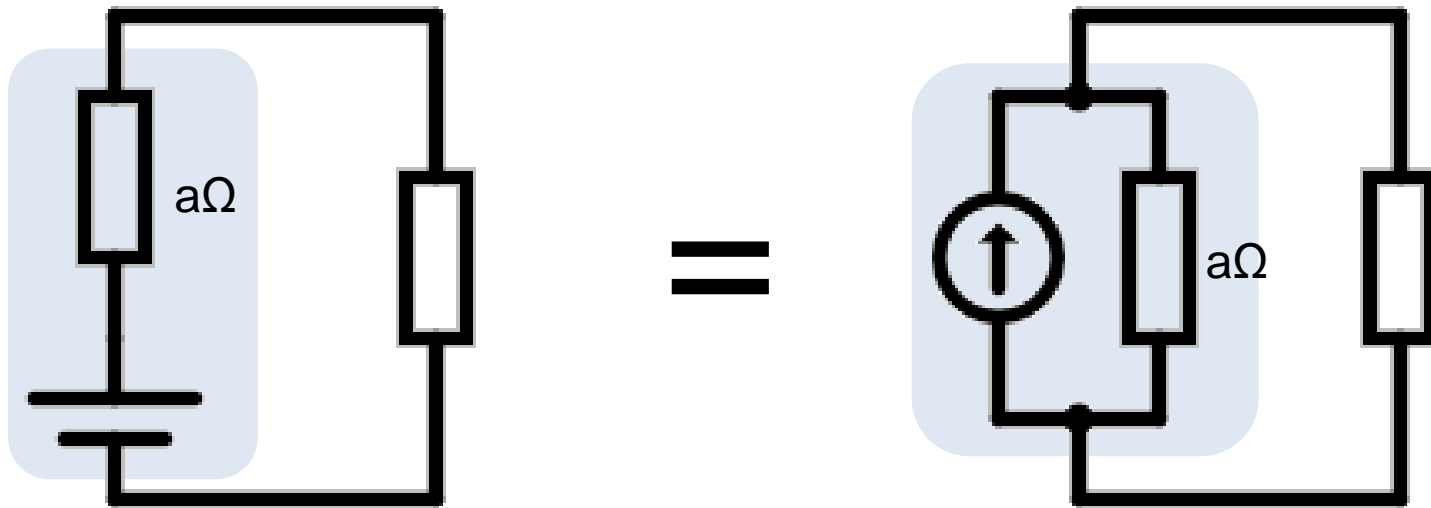


perfect world



reality (due internal resistance)

## Source Conversion



$$I = \frac{V}{a\Omega}$$

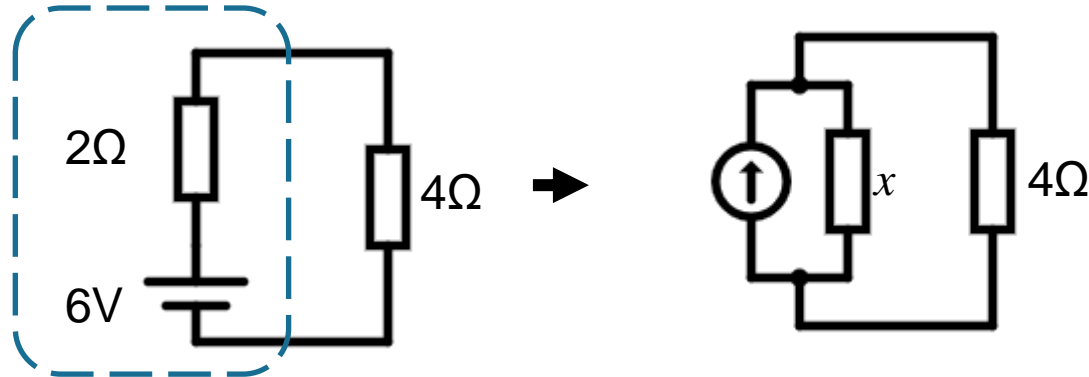
$$V = I \cdot a\Omega$$

---



## Example

*Convert to current source*



Internal resistance is the same for both circuit, so  $x=2\Omega$

Current is equal to voltage source divided by internal resistance, so  $I=6/2=3\text{A}$

Polarity of current source matches the polarity of voltage source

---



## Suggested reading

### Introductory Circuit Analysis

- Kap 5: **5.6 - 5.7**, 5.8 - 5.12, 5.14
- Kap 6: **6.5 - 6.7**, 6.8 - 6.9, 6.12
- Kap 7: **7.2 - 7.8**
- Kap 8: 8:9

The book does not have a good material about depended sources 😞

- Kretsanalysis by Bill Karlström p.19-20 (see last page of the slides)



## Suggested exercises

- Kap 5: 25, 27
  - Kap 6: 27, 31
  - Kap 7: 3, 9, 11, 13, 23
  - Kap 8: 65, 69
-

## Beroende energikällor

I beroende energikällor är källströmmen eller källspänningen beroende av andra storheter i kretsen.

Beroende energikällor används för att modellera transistorer och förstärkare.

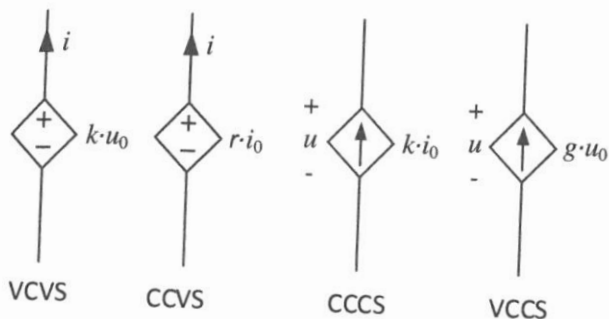


Fig 2.10 Beroende energikällor

### VCVS

Spänningsberoende spänningskälla. Dess källspänning beror av en spänning  $u_0$  någon annanstans i kretsen oberoende av strömmen  $i$ .

Konstanten  $k$  är enhetslös.

### CCVS

Strömberoende spänningskälla. Dess källspänning beror av en ström  $i_0$  någon annanstans i kretsen oberoende av strömmen  $i$ .

Konstanten  $r$  har enheten  $\Omega$ .

### CCCS

Strömberoende strömkälla. Dess källström beror av en ström  $i_0$  någon annanstans i kretsen oberoende av spänningen  $u$ .

Konstanten  $k$  är enhetslös.

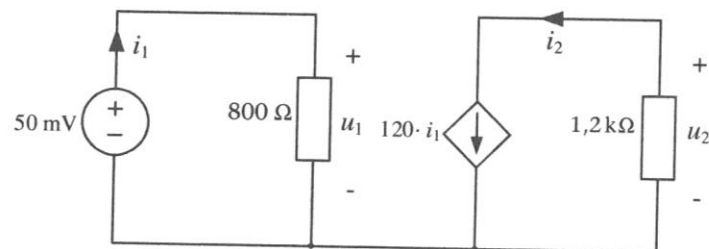
### VCCS

Spänningsberoende strömkälla. Dess källström beror av en spänning  $u_0$  någon annanstans i kretsen oberoende av spänningen  $u$ .

Konstanten  $g$  har enheten  $S = \text{siemens} = \Omega^{-1}$ .

### Exempel 2.7

Bestäm spänningen  $u_2$  i kretsen nedan (enkel transistormodell).



### Lösning

Spänningen  $u_1$  över  $800 \Omega$ -resistorn är 50 mV. Detta ger

$$i_1 = \frac{50 \cdot 10^{-3}}{800} = 62,5 \mu\text{A} \quad (2.34) \quad (\text{strömmen } i_1 \text{ in vid plus}).$$

Detta ger

$$i_2 = 120 \cdot i_1 = 120 \cdot 62,5 \cdot 10^{-6} = 7,5 \text{ mA} \quad (2.35)$$

så att

$$u_2 = -1,2 \cdot 10^3 \cdot i_2 = -1,2 \cdot 10^3 \cdot 7,5 \cdot 10^{-3} = \underline{\underline{-9 \text{ V}}} \quad (2.36)$$

Observera minustecknet! Detta kommer av att strömmens referensriktning är in mot minustecknet!!