Visualization, DD2257
Prof. Dr. Tino Weinkauf

## Data Description

Sampled Data




- In most cases, the visualization data represents a continuous real object, e.g., an oscillating membrane, a velocity field around a body, an organ, human tissue, etc.
- This object lives in an n-dimensional space - the domain (aka. observation space)
- Usually, the data is only given at a finite set of locations, or samples, in space and/or time
- Remember imaging processes like numerical simulation and CT-scanning, note similarity to pixel images
- We call this a discrete representation of a continuous object


## Discrete Representations

We usually deal with the reconstruction of a continuous real object from a given discrete representation.


## Discrete Representations

We usually deal with the reconstruction of a continuous real object from a given discrete representation.

Samples are connected to each other to form grids / meshes, covering the entire domain.


## Grid terminology

grid cell: largest-dimensional element in a grid
2D: grid face
3D: grid voxel


## Operations on Grids

- Determine the data value at a position
- Easy at the grid vertices
- At other positions: Interpolation Schemes
- Determine neighbors
- Convert to other grid types
- Compute metrics
- Distance, Area, Volume
- Compute Bounding Box


## Data Connectivity

- There are different types of grids:
- Structured grids
connectivity is implicitly given.
- Block-structured grids combination of several structured grids
- Unstructured grids connectivity is explicitly given.
- Hybrid grids
combination of different grid types


## Structured grids

- "Structured" refers to the matrix-like connectivity between the grid vertices
- We distinguish different types of structured grids regarding the alignment to the coordinate system and the size of cells

uniform grid axis-aligned, identical cells implicitly given coordinates

rectilinear grid
axis-aligned, cells different size semi-implicitly given coordinates

curvilinear grid not axis-aligned, cells different size explicitly given coordinates


## Structured grids

- Number of grid vertices: $n_{x}, n_{y}, n_{z}$
- We can address every grid vertex with an index tuple (i, j, k)
- $0 \leq i<n_{x}$
$0 \leq j<n_{y}$
$0 \leq k<n_{z}$
 axis-aligned, identical cells implicitly given coordinates

rectilinear grid
axis-aligned, cells different size semi-implicitly given coordinates



## Structured grids

- Number of grid vertices: $n_{x}, n_{y}, n_{z}$
- We can address every grid cell with an index tuple (i, j, k)
- $0 \leq i<n_{x}-1$
$0 \leq j<n_{y}-1$
$0 \leq k<n_{z}-1$
- $\rightarrow$ Number of cells: $\left(n_{x}-1\right) \times\left(n_{y}-1\right) \times\left(n_{z}-1\right)$

axis-aligned, identical cells implicitly given coordinates

rectilinear grid
axis-aligned, cells different size semi-implicitly given coordinates

not axis-aligned, cells different size explicitly given coordinates


## Regular or uniform grids

- Cells are rectangles or rectangular cuboids of the same size
- All grid lines are parallel to the axes

- To define a uniform grid, we need the following:
- Bounding box: $\left(x_{\min }, y_{\min }, z_{\min }\right)-\left(x_{\max }, y_{\max }, z_{\max }\right)$
- Number of grid vertices in each dimension: $n_{x}, n_{y}, n_{z}$
$\rightarrow$ from that information we can derive the Cell size: $d_{x}, d_{y}, d_{z}$


## Regular or uniform grids

- Well suited for image data (medical applications)
- Coordinate $\rightarrow$ cell is very simple and cheap
- Global search is good enough; local search not required

- Coordinate of a grid vertex:

$$
\left(i \cdot d_{x}, j \cdot d_{y}, k \cdot d_{z}\right)+\left(x_{\min }, y_{\left.\min , z_{\min }\right)}\right.
$$



## Cartesian grid

- Special case of a uniform grid: $d_{x}=d_{y}=d_{z}$
- Consists of squares (2D), cubes (3D)



## Rectilinear grids

- Cells are rectangles of different sizes
- All grid lines are parallel to the axes
- Vertex locations are inferred from positions
 of grid lines for each dimension:
- XLoc $=\{0.0,1.5,2.0,5.0, \ldots\}$
- YLoc $=\{-1.0,0.3,1.0,2.0, \ldots\}$
- ZLoc = \{3.0, 3.5, 3.6, 4.1, ...\}
- Coordinate $\rightarrow$ cell still quite simple



## - Curvilinear grids

- Vertex locations are explicitly given
- XYZLoc $=\{(0.0,-1.0,3.0),(1.5,0.3,3.5),(2.0,1.0,3.6), \ldots\}$
- Cells are quadrilaterals or cuboids
- Grid lines are not (necessarily) parallel to the axes


2D curvilinear grid


3D curvilinear grids


## - Curvilinear grids

- Coordinate $\rightarrow$ cell:
- Local search within last cell or its immediate neighbors
- Global search via quadtree/octree



## Data structures for structured grids



- dependent variable: array
- positions: $2 / 3$ location vectors
rectilinear grid
- dependent variable: array
- positions: array


## curvilinear grid

## - Block-structured grids

- combination of several structured grids

- Demands on data storage, an example:

- Demands on data storage, an example:



## Unstructured Grids

sample points are not laid out in a matrix-like fashion
unstructured grids connect neighboring samples
many possibilities how to do this

triangle/tetrahedral mesh<br>2D/3D linear cells<br>quad/hexahedral mesh<br>2D/3D cube-like cells



## Unstructured Grids: Triangle / Tetrahedral Meshes



2D unstructured grid consisting of triangles


3D unstructured grid consisting of tetrahedra (from TetGen user manual)

## Unstructured Grids

Vertex locations and connectivity explicitly given Coordinate $\rightarrow$ cell:

- Local search within last cell or its immediate neighbors
- Global search via quadtree/octree



## Data structures for Triangles Meshes

shared vertex data structure
vertex table
stores positions

from this we can derive:
list of edges
vertex neighbors
$12 B / v+12 B / f=36 B / v$ no neighborhood info

## Data structures for Triangles Meshes

many other options exist



120 B/v
edge orientation?

| Triangles |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{x}_{11}$ | $\mathrm{y}_{11}$ | $\mathrm{z}_{11}$ | $\mathrm{x}_{12}$ | $\mathrm{y}_{12}$ | $\mathrm{z}_{12}$ | $\mathrm{x}_{13}$ | $\mathrm{y}_{13}$ | $\mathrm{z}_{13}$ |
| $\mathrm{x}_{21}$ | $\mathrm{y}_{21}$ | $\mathrm{z}_{21}$ | $\mathrm{x}_{22}$ | $\mathrm{y}_{22}$ | $\mathrm{z}_{22}$ | $\mathrm{x}_{23}$ | $\mathrm{y}_{23}$ | $\mathrm{z}_{23}$ |
|  | $\ldots$ |  | $\ldots$ |  |  | $\ldots$ |  |  |
| $\mathrm{x}_{\mathrm{P} 1}$ | $\mathrm{y}_{\mathrm{P} 1}$ | $\mathrm{z}_{\mathrm{P} 1}$ | $\mathrm{x}_{\mathrm{P} 2}$ | $\mathrm{y}_{\mathrm{F} 2}$ | $\mathrm{z}_{\mathrm{P} 2}$ | $\mathrm{x}_{\mathrm{P} 3}$ | $\mathrm{y}_{\mathrm{P} 3}$ | $\mathrm{z}_{\mathrm{F} 3}$ |

36 B/f = 72 B/v
no connectivity!


96 to 144 B/
no case distinctions during traversal

## Unstructured Grids: Quad Mesh



2D unstructured grid consisting of quads

## Hybrid Grids

Combination of different grid types


## Summary

- Continuous objects are often the subject of study
- Need to be sampled to be represented in the computer
- Data is stored at samples (most often points)
- Structured grids: matrix-like organization of neighborhood
- uniform
- rectilinear
- curvilinear
- Unstructured grids: arbitrary organization of neighborhood
- triangle/tetrahedral meshes
- quad/hexahedral meshes

